

CP Model for Assembly Line Balancing and Scheduling with Walking Workers and Parallel Stations

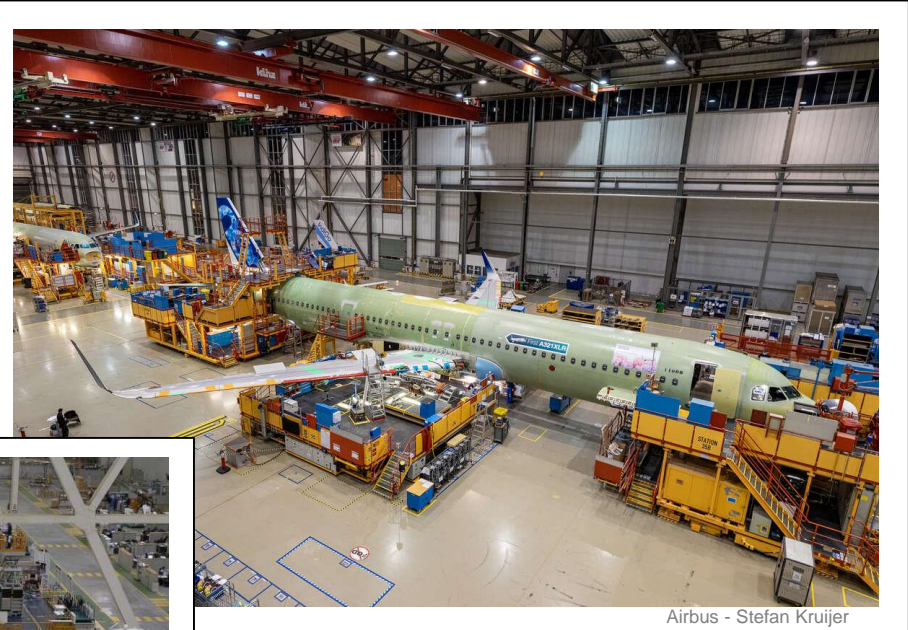
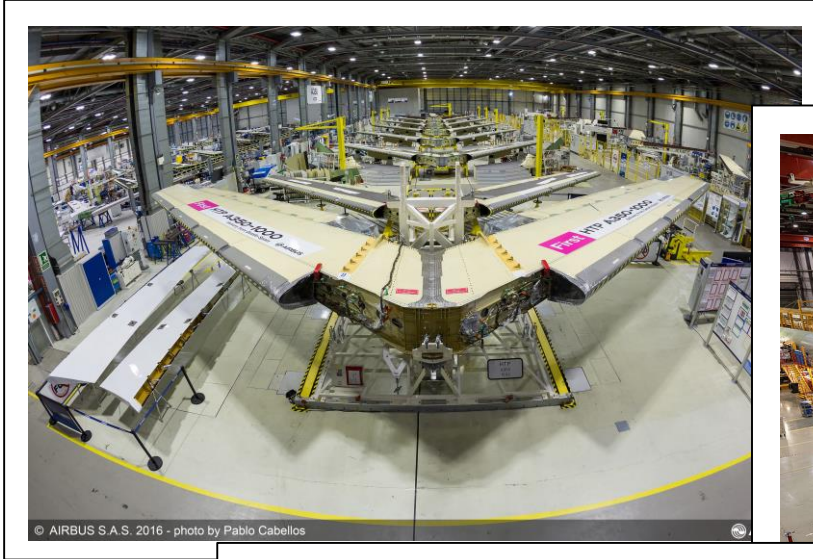
Xavier Pucel, Stéphanie Roussel

xavier.pucel@onera.fr, stephanie.roussel@onera.fr

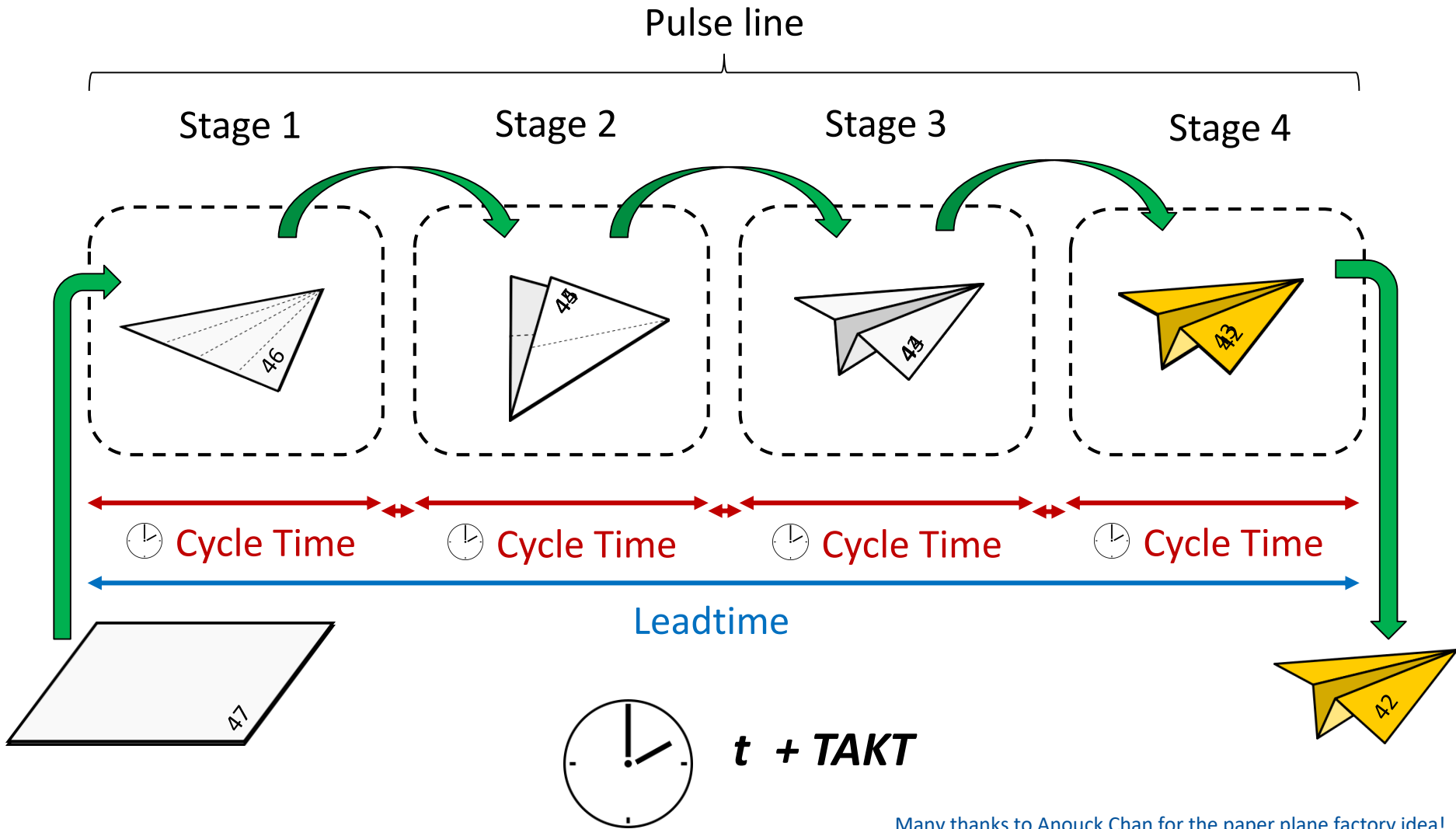


Application Track

Pulse Assembly Line – In Real Life

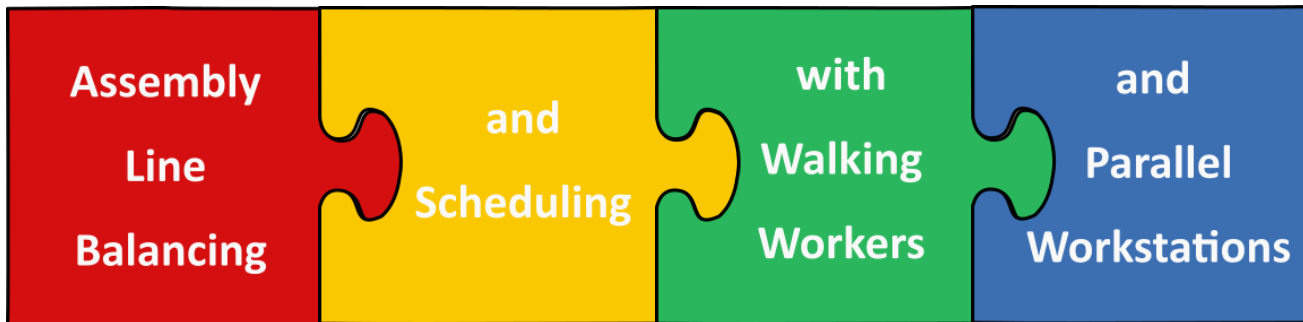
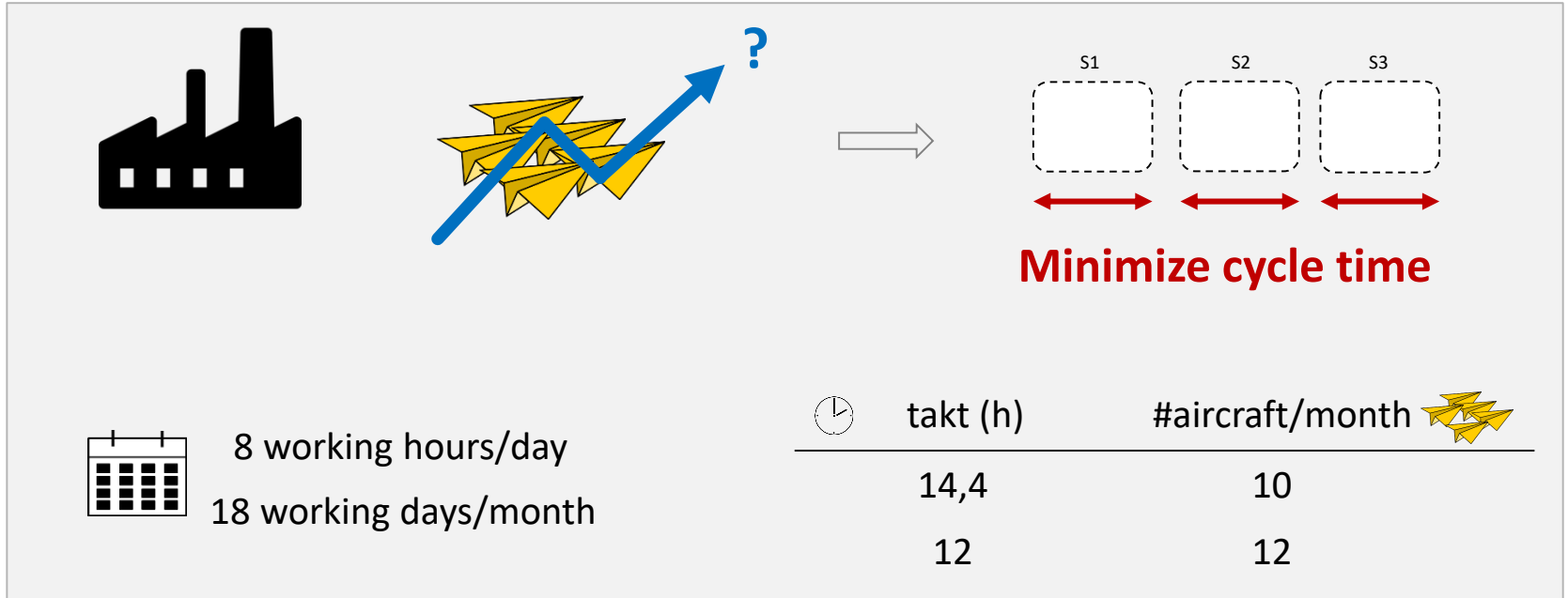


Pulse Assembly Line - Model



Many thanks to Anouck Chan for the paper plane factory idea!

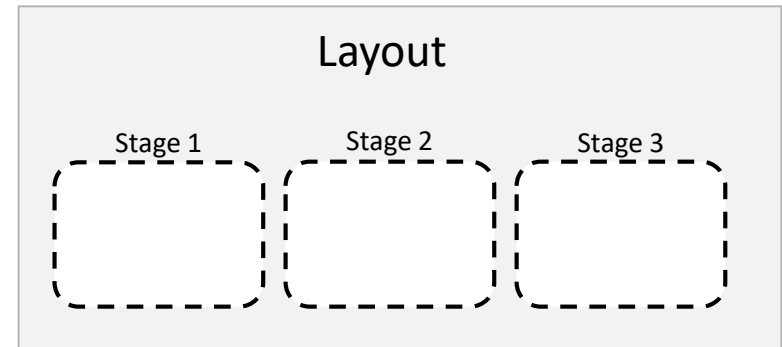
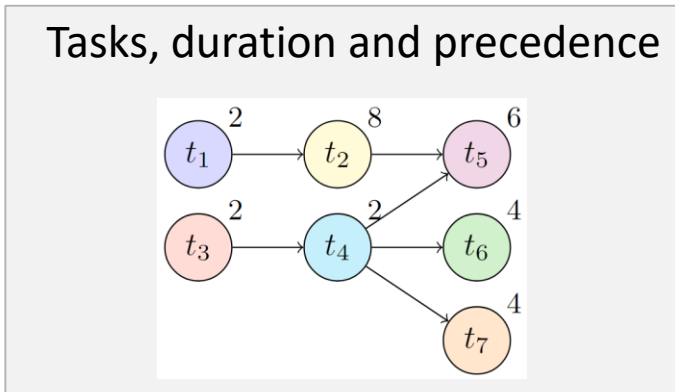
Our Problem



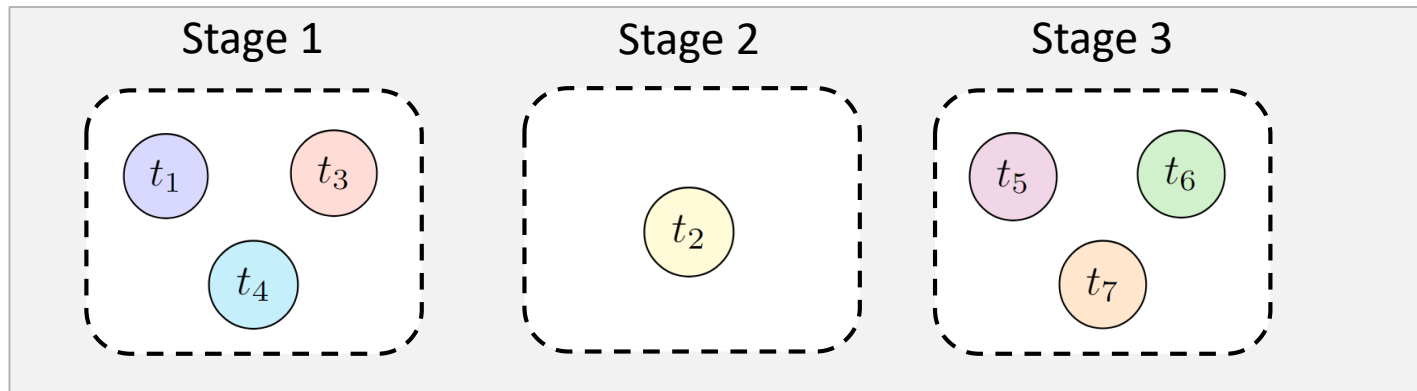
AL Balancing (ALB)



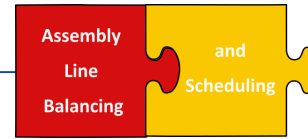
Input



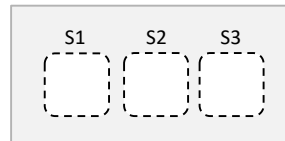
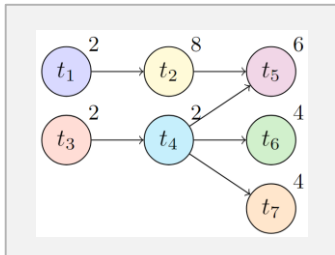
Solution



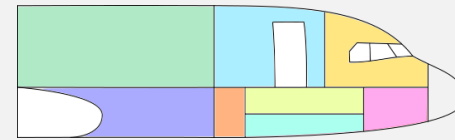
ALB & Scheduling



Input



Zones with max. capacity

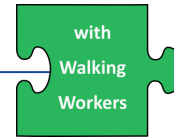


One cumulative resource per zone

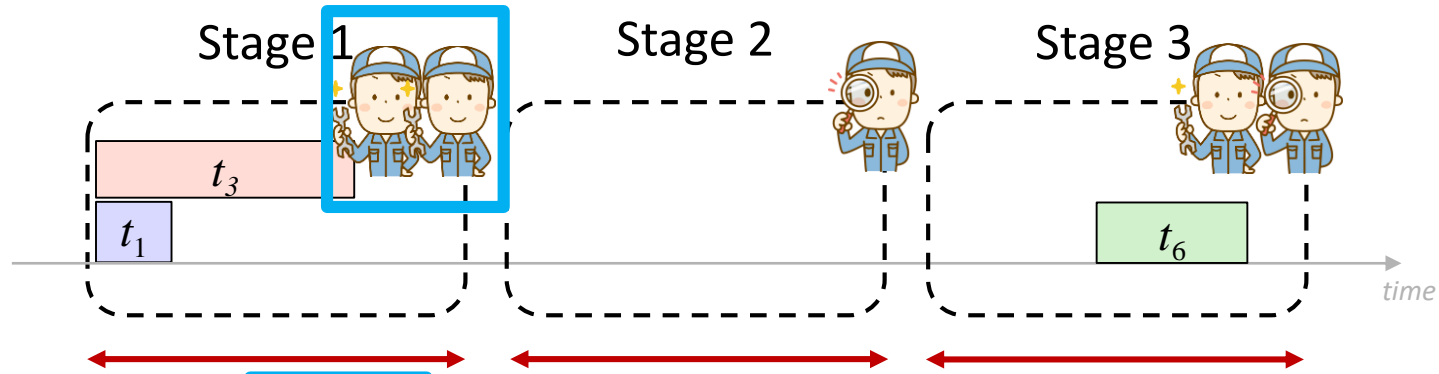
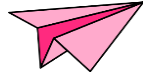
Solution

	Stage 1		Stage 2		Stage 3	
Zone 1	t_1		t_2		t_6	t_5
Zone 2	t_3		t_4		t_7	

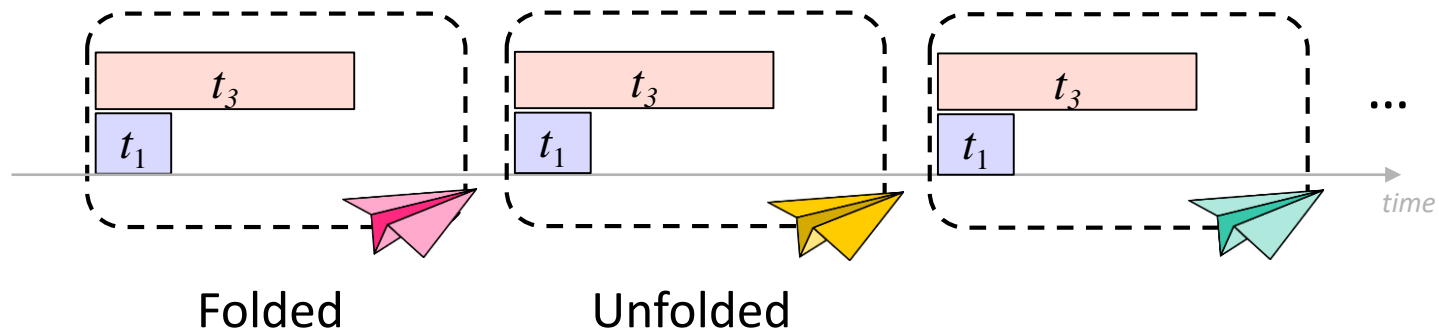
(Non Walking) Workers



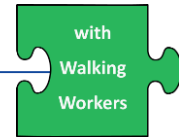
Aircraft schedule



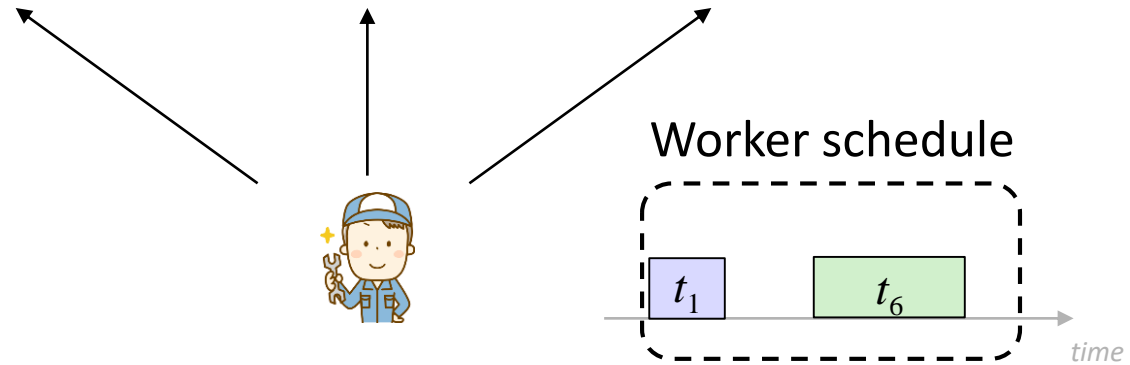
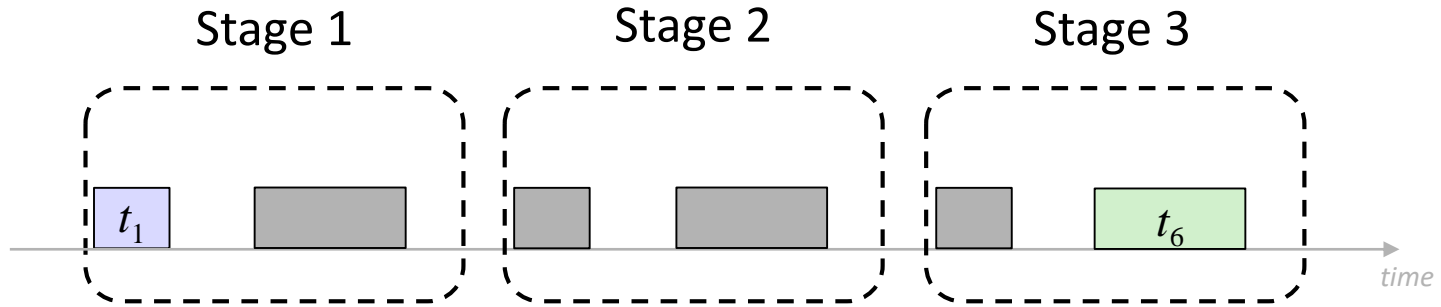
Workers schedule



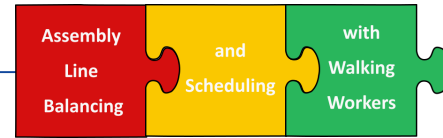
Walking Workers



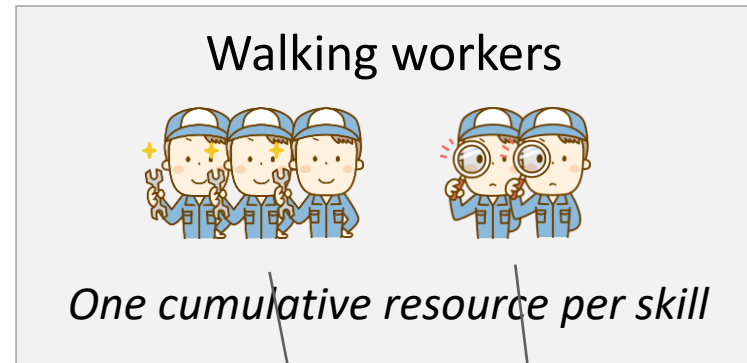
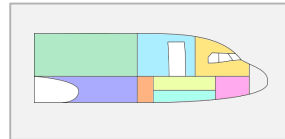
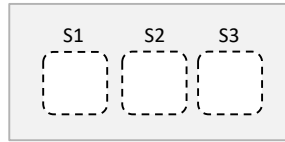
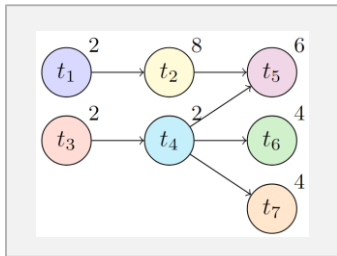
Aircraft schedule 



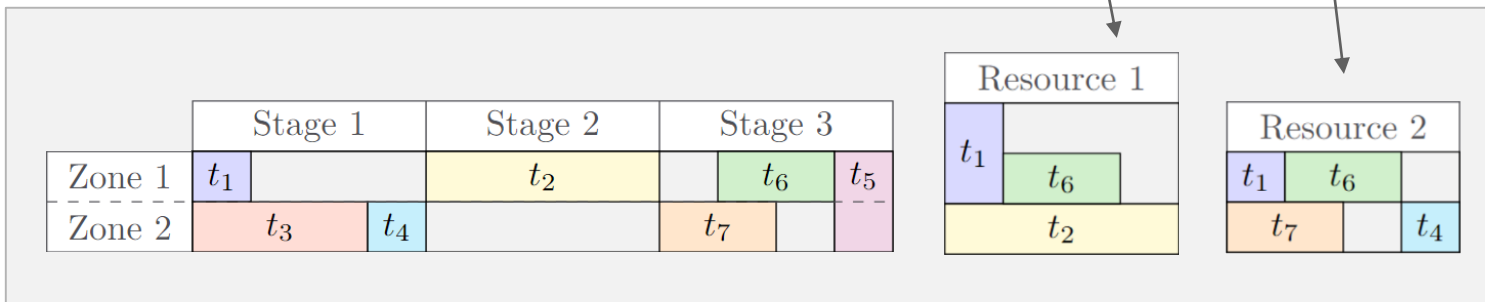
ALB & Scheduling with Walking Workers



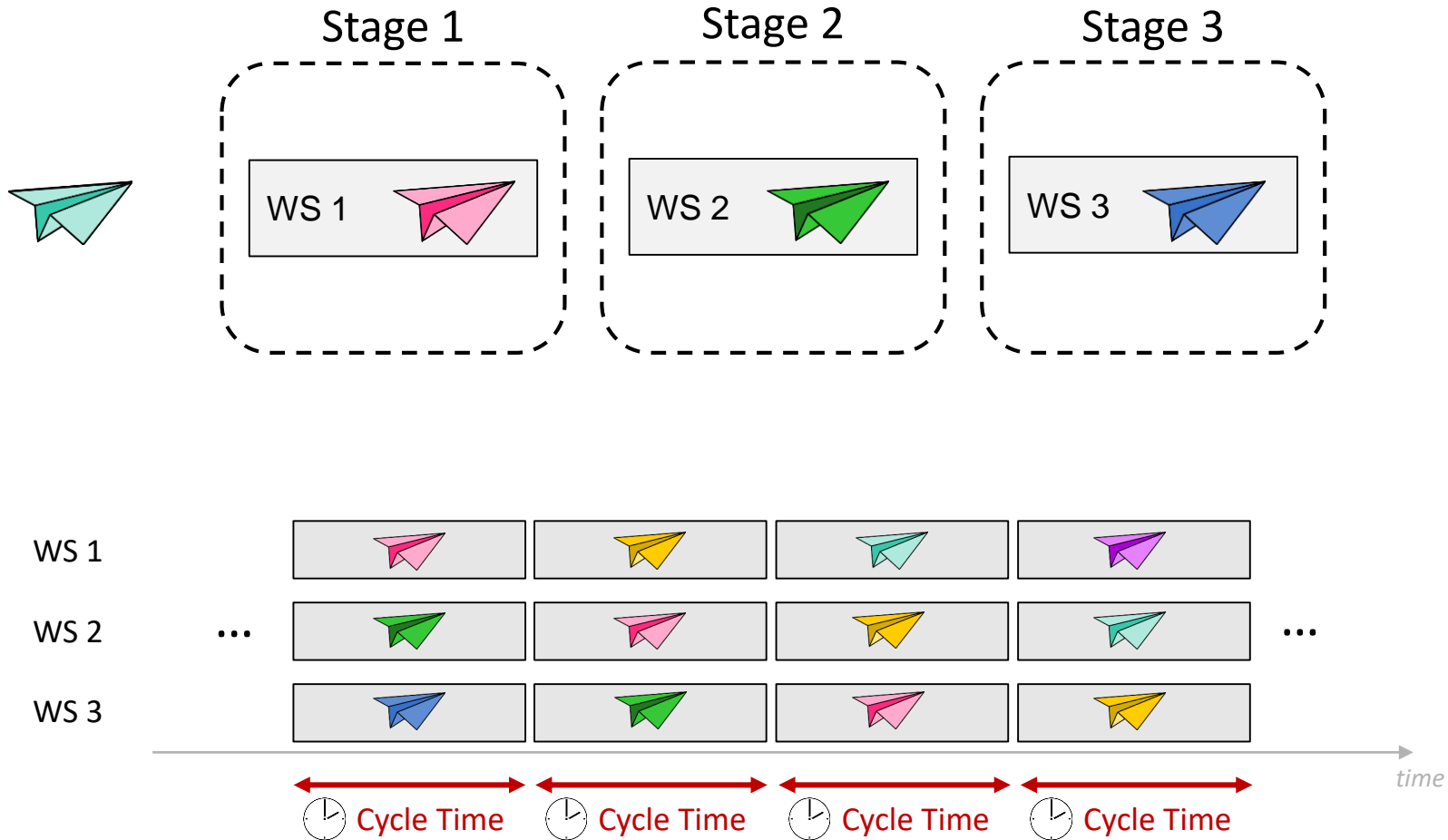
Input



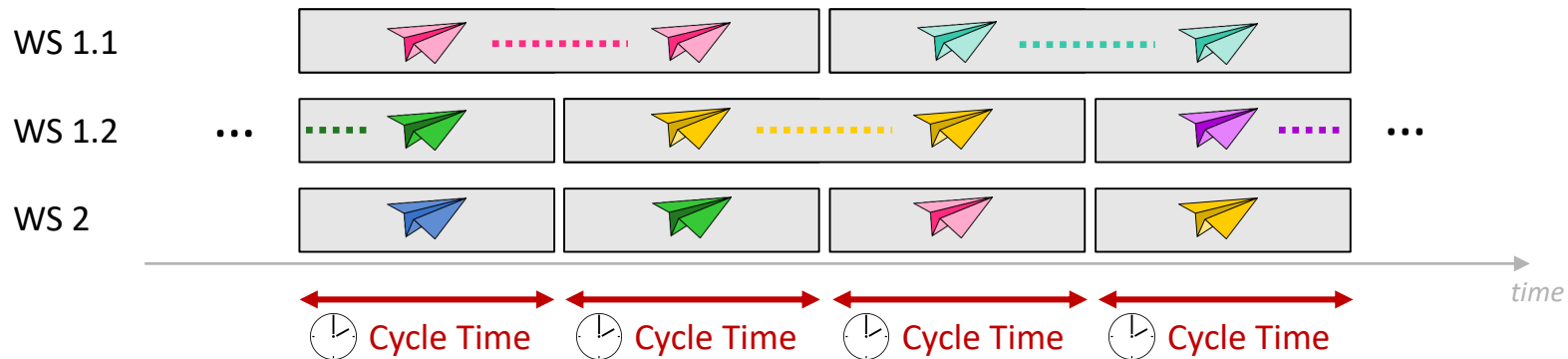
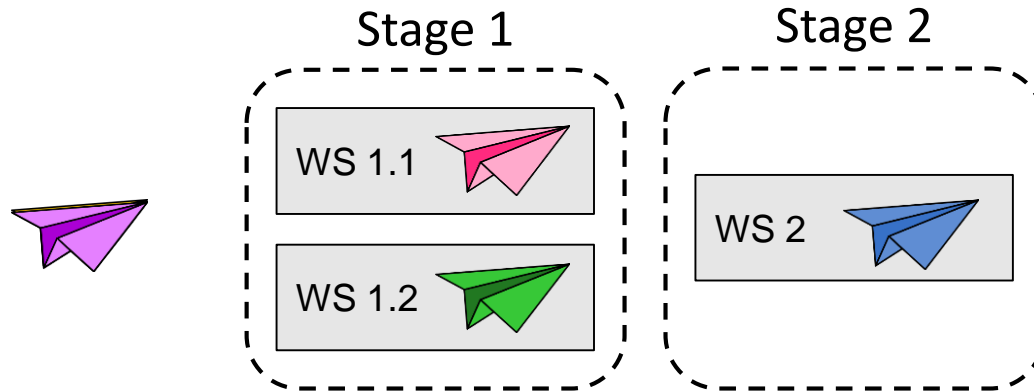
Solution



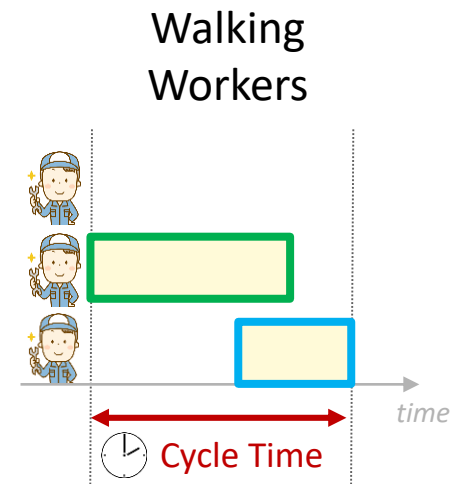
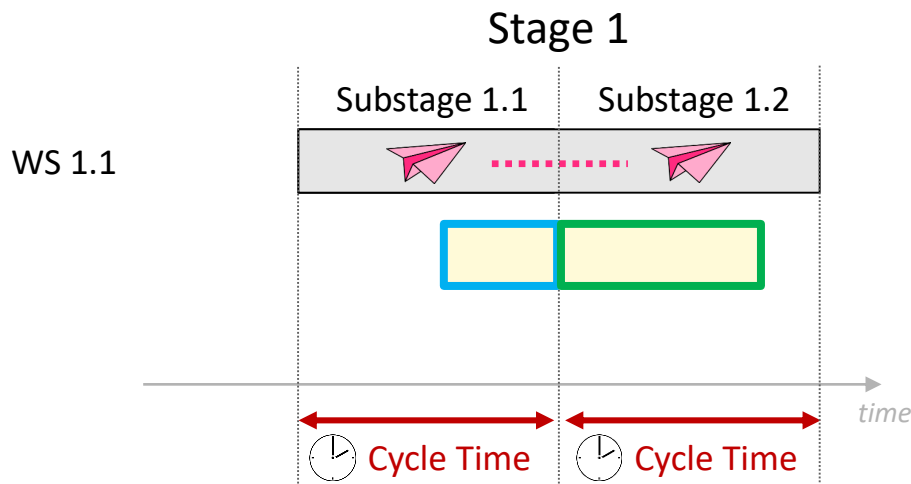
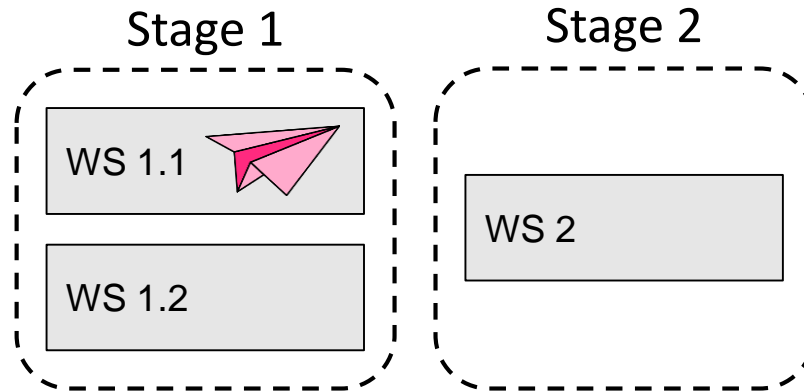
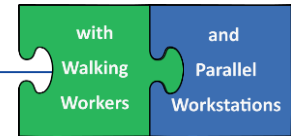
Parallel Workstations



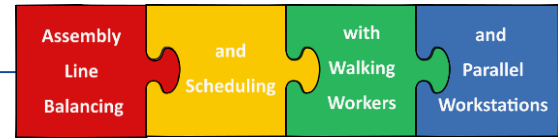
Parallel Workstations



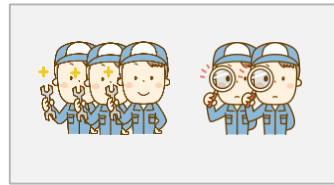
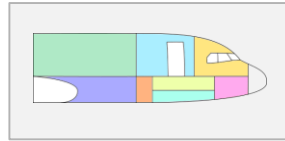
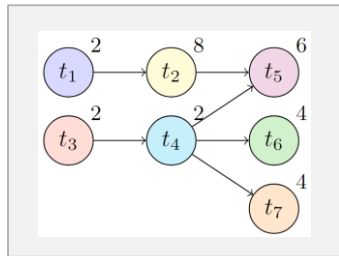
Parallel Workstations



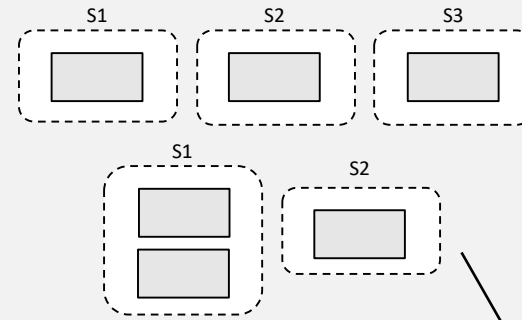
ALB & Scheduling with Walking Workers and Parallel Workstations



Input



Layouts with parallel workstations



Solution

	Stage 1	Stage 2	Stage 3
Zone 1	t ₁	t ₂	t ₆ , t ₅
Zone 2	t ₃ , t ₄		t ₇

t ₁	t ₆
t ₂	

t ₁	t ₆
t ₇	t ₄

Cycle Time = 8

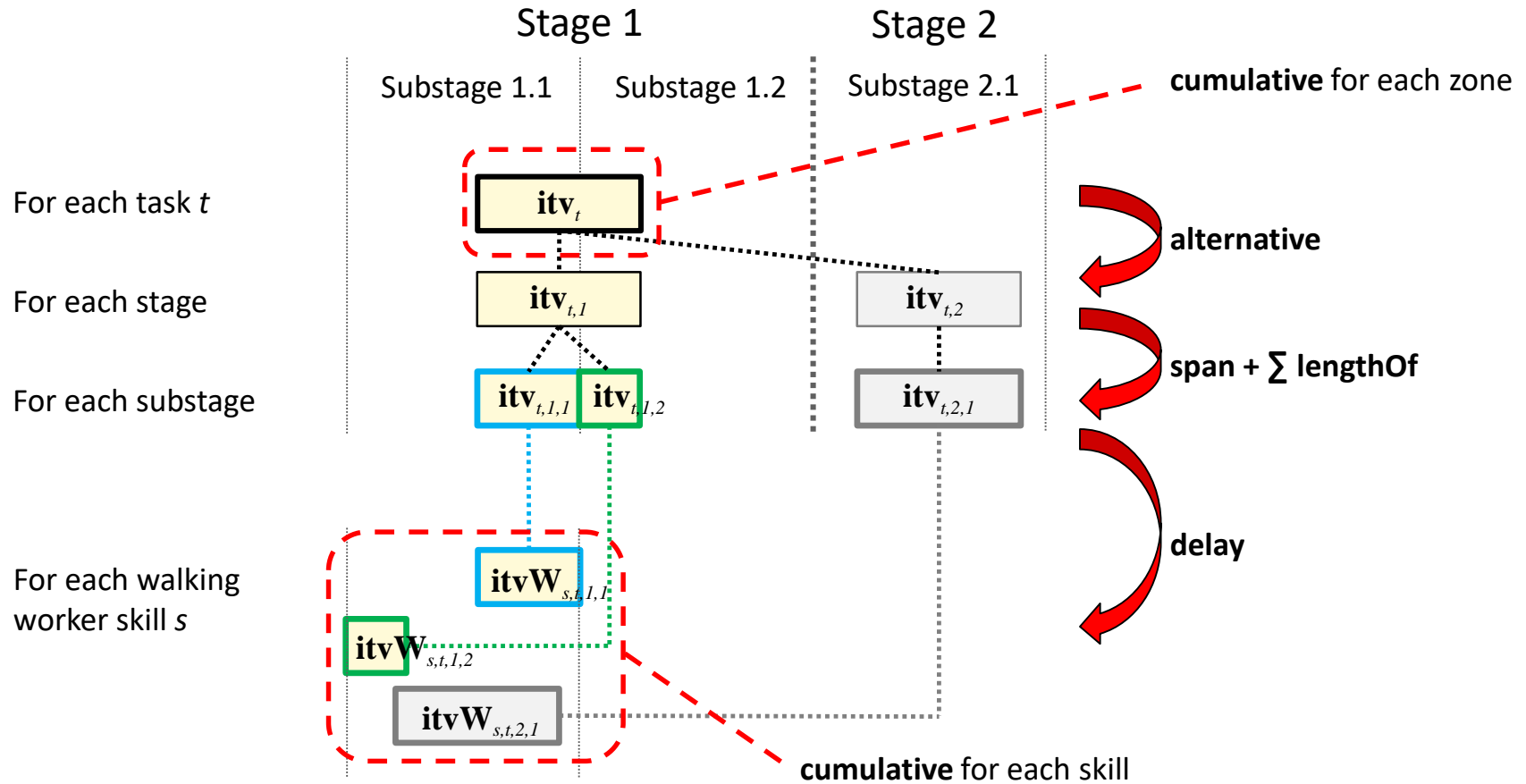
	Stage 1		Stage 2
	Substage 1.1	Substage 1.2	Substage 2.1
Zone 1	t ₁	t ₂ , t ₅	t ₆
Zone 2	t ₃ , t ₄		t ₇

t ₂	
t ₁	t ₂ , t ₆

t ₁	t ₇
t ₄	t ₆

Cycle Time = 6

Constraint Programming Encoding – Overview

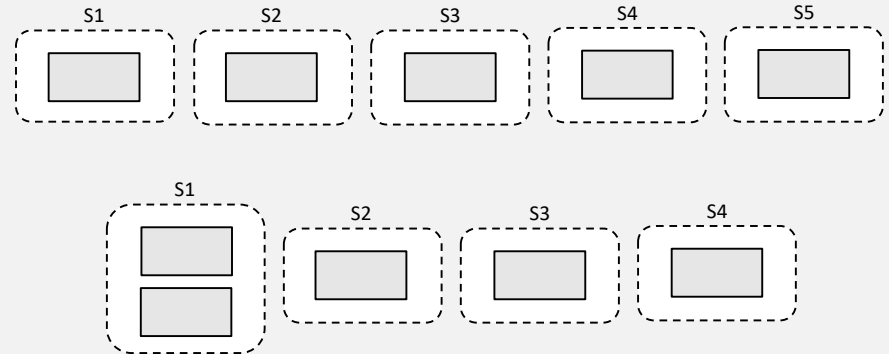


Experiments – Overview

- 3 sets of benchmarks:
 - original industrial dataset (anonymous)
 - adapted industrial dataset (public)
 - generated academic dataset (public)
- IBM CP Optimizer 20.1.10

Aircraft Manufacturer – Small Aircraft Assembly Line

- 51 tasks
- 93 precedence constraints
- 12 work zones
- 23 walking workers
- 2 layouts

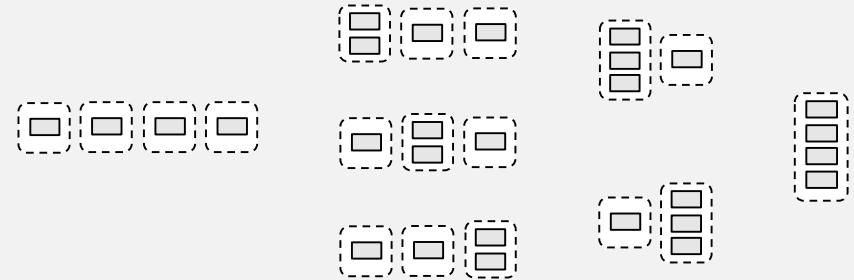


- 30 minutes time-out
- best solution found in a few seconds
- no optimality proof

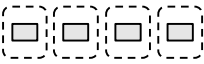



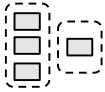
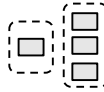

Experiments – Second Dataset (public)

Aircraft Manufacturer – Aircraft Assembly Line

- **21 instances**
- 3 original datasets
- 178 tasks / 628 tasks
- 48 work zones
- 6 walking workers types
- 7 layouts (4 WS)



- 10 minutes time-out



















instances	#tasks							
Ins. 1	178	1260	1260	1260	1260	1024	900	855
Ins. 2	178	1260	-----	1260	1260	-----	954	-----
Ins. 3	628	1200	-----	900	1172	-----	1160	-----

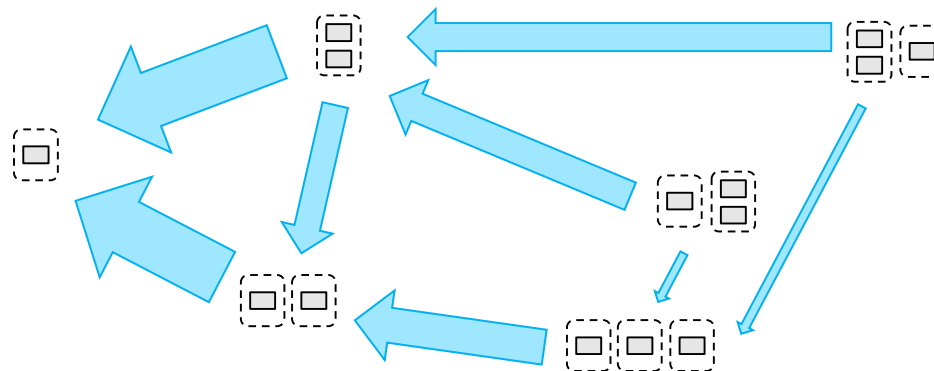
Experiments – Third Dataset (public)

Academic – PSP-based dataset

- 900 instances
- 150 original j30rcp instances
- 30 tasks
- 0 work zone
- 4 walking workers types
- 6 layouts

- 5 minutes time-out

layout	#solved	#optimal	avg. time (s)
			2.5
			72.3
			124.1
			151.1
			193.9
			184.5



What's Next ?

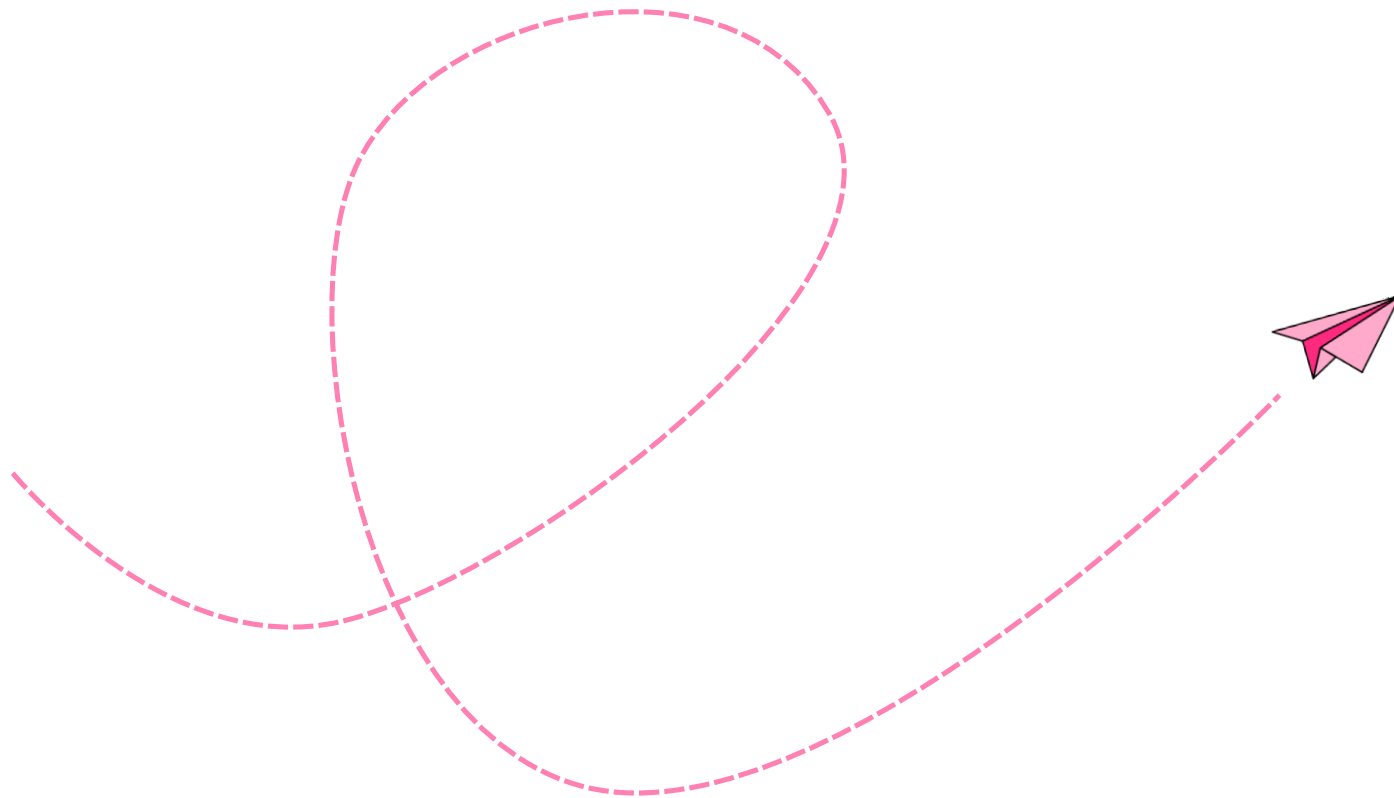
Summary

- New problem and associated datasets
- CP approach

Perspectives

- Other heuristics / solvers / approaches
- Multi-criteria: cycle time and walking workers
- Several aircraft models in the same assembly line





Thank you for your attention

Many thanks to Anouck Chan for the paper plane factory idea!